

# Probabilistic relational models for recommendation systems: review and comparative study

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# Motivation

## Recommender Systems

- Recommender Systems (RSs) are software tools and techniques providing suggestions for items to be of use to a particular user within a specific domain.
- *Examples* : Amazon, YouTube, etc.

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## Recommender Systems

- Recommender Systems (RSs) are software tools and techniques providing suggestions for items to be of use to a particular user within a specific domain.
- *Examples* : Amazon, YouTube, etc.

## Recommendation techniques

- Collaborative filtering
- Content-based
- Demographic
- ...

# Motivation

## Major Challenges

- Scalability - undegraded performance with growing data
- Data sparsity - Sparse User-Item matrix
- Cold start problem - ability to perform recommendation for new user/item or in a new system

## Existing techniques drawbacks

# Motivation

## Major Challenges

### Existing techniques drawbacks

- rely on propositional data representation.
- do not exploit all the available information :
  - Collaborative-based approaches are based on the user-item matrix.
  - Content-based approaches are based on the users profiles.
  - ...

### Hybrid methods

# Motivation

## Major Challenges

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## Hybrid methods

Showed better performance than standard techniques.

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- More expressive classes of directed graphical models have emerged to extract statistical patterns from relational data.

## Relational datamining models

Performing recommendation using a relational model :  
*Probabilistic Relational Models (Koller and Pfeffer 1998)*

# Outline

- 1 Probabilistic relational models
- 2 Recommendation using PRMs
- 3 Implementation
- 4 Conclusion & perspective

# Outline...

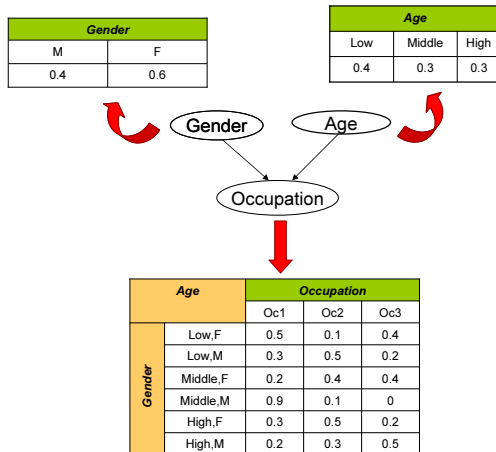
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# Bayesian networks (*Pearl 1988*)

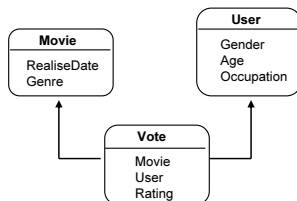
## Definition

A BN is composed of 2 components :

- Qualitative : **DAG** over a set of variables.
- Quantitative : set of *CPTs = Conditional Probability Table* of each variable given its parents in the graph.







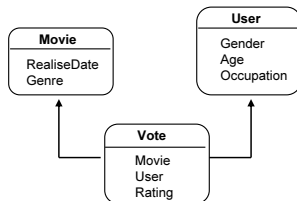
A relational schema  $\mathcal{R}$

- Classes + relational variables.

### An example of a Relational Schema



# Probabilistic Relational Models *(Koller and Pfeffer 1998)*

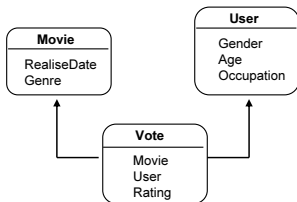


## A relational schema $\mathcal{R}$

- Classes + relational variables.
- Reference slots (e.g., *Vote.Movie*, *Vote.User*).

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# Probabilistic Relational Models *(Koller and Pfeffer 1998)*



*An example of a Relational Schema*

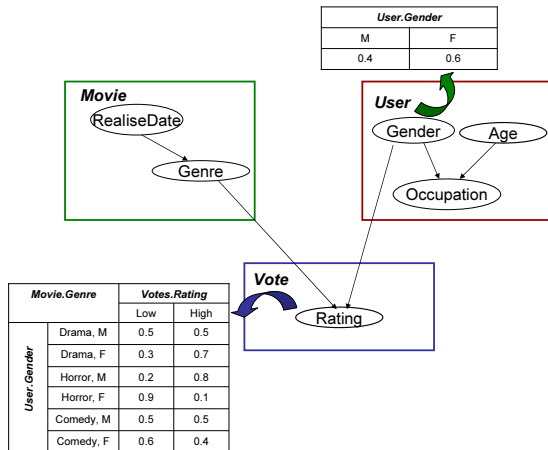
## A relational schema $\mathcal{R}$

- Classes + relational variables.
- Reference slots (e.g., *Vote.Movie*, *Vote.User*).
- Slot chain = A sequence of reference slots
  - Allow to walk in the relational schema to create new variables (e.g., *Vote.User.User<sup>-1</sup>.Movie* : all the movies voted by a particular user.)

# Probabilistic Relational Models *(Koller and Pfeffer 1998)*

## Definition

## Aggregators



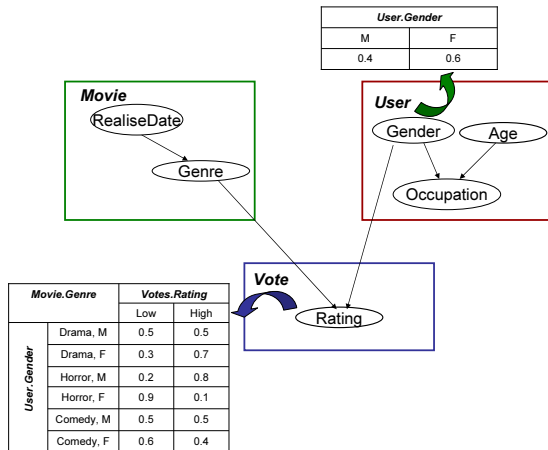
# Probabilistic Relational Models *(Koller and Pfeffer 1998)*

## Definition

A PRM  $\Pi$  for a relational schema  $R$ :

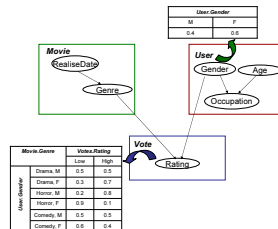
- A qualitative dependency structure  $\mathcal{S}$  (with possible long **slot chains** and **aggregation functions**).
- A set of parameters  $\theta_{\mathcal{S}}$ .

## Aggregators



# Probabilistic Relational Models *(Koller and Pfeffer 1998)*

## Definition



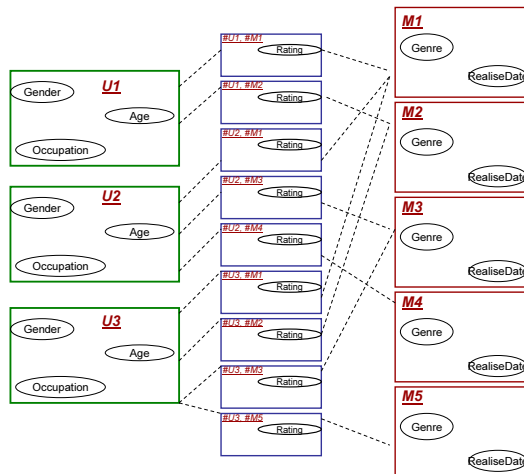
## Aggregators

- $\gamma(\text{Vote.User.User}^{-1}.\text{Movie.genre}) \rightarrow \text{Vote.rating}$  : All the gender of movies voted by a particular user
  - A finite set, not known in advance to create the conditional probability table.
  - Has to be substitute by an aggregated value (e.g.  $(\gamma = \text{MODE})$ ).

# Ground Bayesian Network (1/2)

## GBN

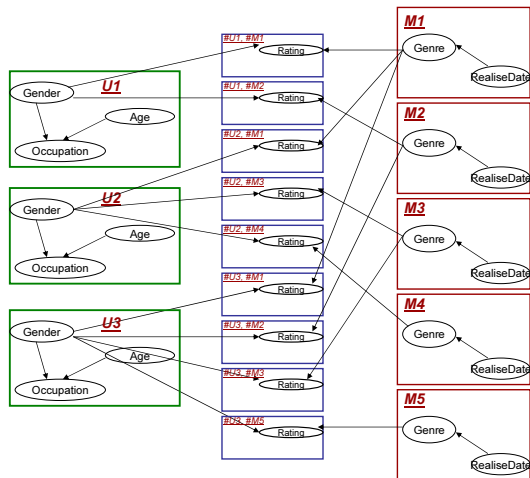
Varies with the relational skeleton that instantiates the model.



# Ground Bayesian Network (2/2)

## GBN

Varies with the relational skeleton that instantiates the model.



# PRMs learning

Close to BN learning.



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- Parameters learning

# PRMs learning

Close to BN learning.

- Parameters learning
- Structure learning **NP-Hard**
  - Probabilistic dependencies may be between two attributes from either the same class or the classes reachable through reference slots.
  - Constraint on slot chain length for adding dependencies.

# PRMs learning

## Existing methods

Only few works have focused on PRMs structure learning [*RGS* (*Getoor et al. 2001*), *RPC*, *RCD* (*Maier et al. 2010, 2013*)].

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## Critics

- Lack of evaluation process, in a common framework.
- Absence of relational benchmarks to evaluate the effectiveness of the proposed approaches.
- Non-existence of random generation process for generating synthetic data.

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# PRM for recommendation

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- Once learnt, PRM can be used to predict new relations without going through existing relations. **Makes it scalable.**
- Learns a model directly from relational data. **Data sparsity is not an issue.**



# Related work

## Existing approaches

- *Getoor et al., 1999* proposed the idea of parameter learning from incomplete data.
- *Newton et al., 2004* defined hPRMs and used it to perform recommendation.
- *Huang et al., 2005* proposed a unified recommender system based on PRM.
- *Gao et al., 2007* Combine PRMs with other machine learning method.

## Critics

# Related work

## Existing approaches

## Critics

- PRMs are either designed for a specific recommendation task or used in a highly basic form due to the intensive computation required by the model estimation process.

## Our objective

# Related work

Existing approaches

Critics

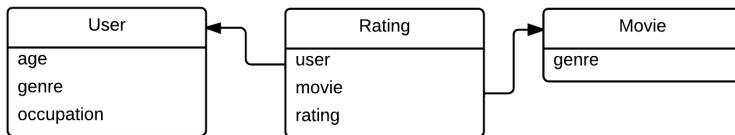
Our objective

Provide efficient PRMs learning techniques : illustrate our development on the recommendation task.

# Steps of our recommendation Process

## Adaptation to *Huang et al.*'s Unified Recommendation Framework

- Combines Collaborative, content-based and demographic filtering into a single framework.
- Our focus on rating data.



**FIGURE :** A relational schema for MovieLens dataset

# Steps of our recommendation Process

- Relational attributes generation

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## • Relational attributes generation

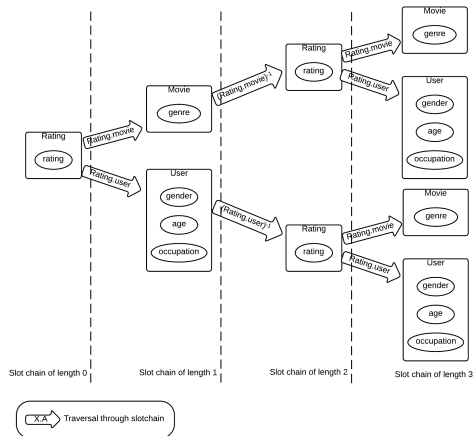


FIGURE : Slot chain traversal

# Steps of our recommendation Process

- Relational attributes generation : Multiset operation

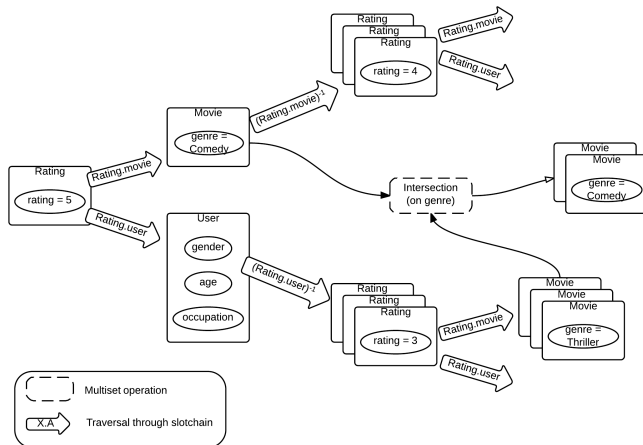


FIGURE : Illustration for multi-set operation

# Steps of our recommendation Process

- Markov Blanket detection
  - Identify the attributes within *Markov Blanket* of the target attribute
  - We are using *IAMB (Incremental Association Markov Blanket, [Tsamardinos et al., 2003])* algorithm with *Mutual Information* as the association measure
- Model creation
  - Heuristic search approach can be used to find the exact structure of the attributes
  - We build a Naïve Bayesian classifier
  - Parameters learning
    - Maximum Likelihood Estimation when enough data
    - Experts' knowledge when insufficient data (new system)



# Steps of our recommendation Process

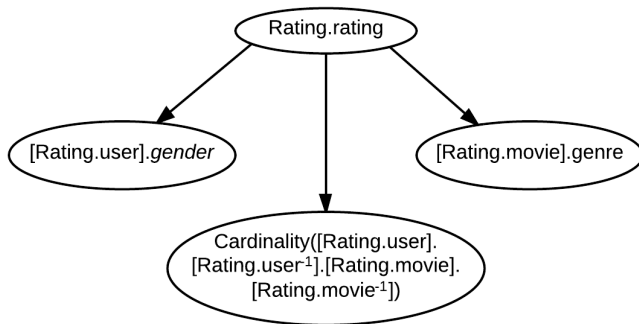


FIGURE : A simple classifier for recommendation

## ● Recommendation

- Predict  $Pr(V|X)$  where  $V$  is the target attribute (`Rating.rating` in our example) and  $X$  are the Markov Blanket attributes

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# Incurred difficulties

## Existing tools

- Almost there is no software tools for manipulating PRMs :
  - Unbbayes : limited to simple PRM models creation and transformation to GBN. No learning methods have been implemented.
  - Proximity : allow the creation and evaluation of some probabilistic models designed for relational knowledge discovery, not PRMs.
  - RCD/RPC : provide only DAPER learning.

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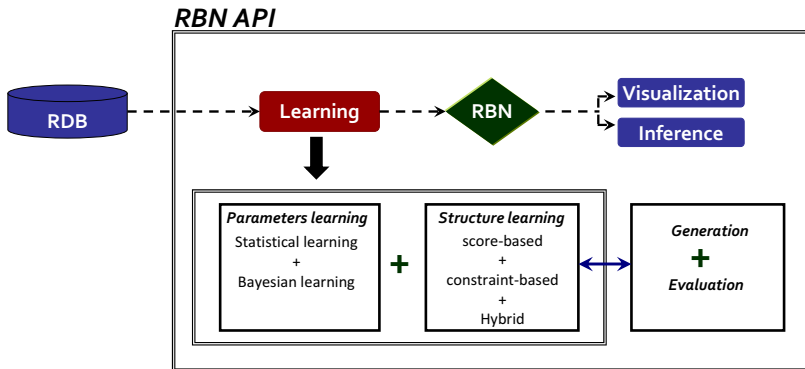
## Solution

Need to develop all from scratch.

# PILGRIM platform

- Implemented in C++ language
- ProBT API for BN basic creation / parameter learning / inference
- Boost graph library

# PILGRIM platform



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# Conclusion

- Use PRM to combine simple models – Demographics / Items' features.
- Capable of providing recommendations for new users.
- Can be made capable of providing recommendations in a new system.
- Longer slot chains for collaborative filtering.
- Multiset operations for better attributes.



# Perspective

- Use of long slot chains and integration with multiset operators.
- Evaluation on multiple datasets.
- Comparison based on performance metrics.

***THANK YOU!***



Any question ?

# Outline...

## 5 Annexes

# Evaluation

- Top-N recommendation method
  - Items are ranked on the basis of the probability of getting high ratings
  - Top N items are recommended and compared with the user's actual preference
  - Average metrics over all users

# Evaluation

- Metrics :

$$\text{Precision}(P) = \frac{\text{Number of hits}}{N} \quad (1a)$$

$$\text{Recall}(R) = \frac{\text{Number of hits}}{\text{Number of high rated movies in the test set}} \quad (1b)$$

$$\text{F-measure}(F) = \frac{2 \times P \times R}{P + R} \quad (1c)$$

where *hits* is the number of actual preferences that appear in the top-N recommendations.

# Evaluation

- Dataset – MovieLens dataset
  - 80% train set, 20% test set
  - 2 type of test sets – General test set and test data for coldstart situation

# Result

- 2 models
  - Rating.user.gender, Rating.user.age, Rating.movie.genre*
  - Rating.user.gender, Rating.user.age, Rating.user.occupation, Rating.movie.genre*

Test set	Model	N = 10			N = 20		
		P	R	F-M	P	R	F-M
General	Model 1	0.0176	0.0203	0.0186	0.0245	0.0376	0.0279
Coldstart	Model 1	0.0200	0.0200	0.0200	0.0250	0.0268	0.0258
General	Model 2	0.0588	0.0247	0.0213	0.0735	0.0551	0.0393
Coldstart	Model 2	0.0200	0.0200	0.0200	0.0350	0.0350	0.0350